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S.E. (Computer Engineering/IT) (II Sem.) EXAMINATION, 2017 ENGINEERING MATHEMATICS—III

(2015 **PATTERN**)

Time: Two Hours

Maximum Marks: 50

- N.B. :— (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8.
 - (ii) Neat diagrams must be drawn wherever necessary.
 - (iii) Figures to the right indicate full marks.
 - (iv) Your answers will be valued as a whole.
 - (v) Use of electronic pocket calculator is allowed.
 - (vi) Assume suitable data, if necessary.
- 1. (a) Solve any two of the following:

[8]

- (i) $\frac{d^2y}{dx^2} y = \frac{2}{1 + e^x}$ (use method of variation of parameters)
- (ii) $(D^2-4)y = e^{4x} + 2x^3$
- (iii) $(2x+1)^2 \frac{d^2y}{dx^2} 2(2x+1) \frac{dy}{dx} 12y = 24x$

P.T.O.

Solve the following integral equation using Fourier transform: [4] (b)

$$\int_0^\infty f(x)\sin \lambda x d\lambda = 1 - \lambda, \ 0 \le \lambda \le 1$$
$$= 0 \quad , \ \lambda \ge 1$$

An electrical circuit consists of an inductance 0.1 henry, a 2. (a) registance R of 20 ohms and a condenser of capacitance C of 25 microfarads. If the differential equation of electric circuit [4]

$$L\frac{d^2q}{dt^2} + R\frac{dq}{dt} + \frac{q}{C} = 0,$$

then find the charge q and current i at any time t, given that when t=0, q=0.05 columbs and $i=\frac{dq}{dt}=0$.

Solve any one: (b)

[4]

Find: (i)

$$\begin{bmatrix} z^{-1} & 1 \\ (z-4)(z-5) \end{bmatrix}$$

by inversion integral method.

Find stransform of: (ii)

$$f(k) = (k+1) a^k, k \ge 0.$$

Using z transform, solve the following difference equation: [4] (c)

$$f(k+1) + \frac{1}{2}f(k) = \left(\frac{1}{2}\right)^k, \ k \ge 0$$

$$f(0) = 0.$$

$$f(0) = 0$$

The first four moments of a distribution about the value 4 3. (a)of the variable are -1.5, 17, -30 and 108. Find the central moments, β_1 and β_2 [4]By the method of least squares, find the straight line that (b) best fits the following data: [4]y 1 14 2 27 3 4 5 There is a small chance of 1/1000 for any computer produced (c) to be defective. Determine in a sample of 2000 computers, the probability no defective and (i)2 defectives (ii)OrTeam A has a probability of $\frac{2}{3}$ of winning whenever the team 4. (a)plays a particular game. If team A plays 4 games, find the probability that the team wins: [4]exactly two games and (*i*) (ii)at least two games.

P.T.O.

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(b) The lifetime of a certain component has a normal distribution with mean of 400 hours and standard deviation of 50 hours. Assuming a normal sample of 1000 components, determine approximately the number of components whose lifetime lies between 340 to 465 hours. Given:

$$Z = 1.2 \text{ Area} = 0.3849$$

$$Z = 1.3$$
 Area = 0.4032.

(c) Calculate the coefficient of correlation for the following data: [4]

5. (a) Find the directional derivative of a function : $\phi = 2x^2 + 3y^2 + z^2 \quad \text{at } (2, 1, 3)$

in the direction of (i+j+k).

(b) Show that the vector field:

$$\overline{F} = (x+2y+4z)i + (2x-3y-z)j + (4x-y+2z)k$$

is irrotational and hence find a scalar potential function φ such that $\,\overline{F}=\nabla\varphi\,.$

[4]

(c) Find the work done by a force field :
$$\overline{F} = x^2i + (x - y)j + (y + z)k$$

along a straight line from (0, 0, 0) to (2, 1, 2).

Or

Find the directional derivative of: 6. (a)

$$\phi = 4xz^3 - 3x^2y^2z$$
 at $(1, 1, 1)$

in the direction of a vector 3i-2j+k.

Show that (any one): (b)

(i)
$$\nabla \left(\frac{\overline{a}.\overline{r}}{r^3}\right) = \frac{\overline{a}}{r^3} - \frac{3(\overline{a}.\overline{r})\overline{r}}{r^5}$$

where \bar{a} is a constant vector. (ii) $\nabla^4(r^4) = 120$.

$$(ii) \quad \nabla^4(r^4) = 120.$$

Evaluate the integral (c)

[5]

[5]

[4]

[4]

along the curve x = y = z = t from t = 0 to t = 2 where

$$\overline{F} = (x^2 + yz)i + (y^2 + zx)j + (z^2 + xy)k$$

7. If (a)

$$u = 3x^2y - y^3$$

find v such that f(z) = u + iv is analytic.

(b) Evaluate:

[5]

$$\oint \frac{z+4}{(z+1)(z+2)} dz$$
e circle $|z| < 3$.

where C is the circle |z| < 3.

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P.T.O.

Find the bilinear transformation which maps the points (c) (1, i, -1) from the z plane into the points (i, 0, -i) of the w plane. [4]

8. (a)If

[4]

$$u = 3x^2 - 3v^2 + 2v$$

find v such that f(z) = u + iv is analytic. Determine f(z) in terms

(b) Evaluate:

[5]

$$\oint_C \frac{Az^2 + z}{z^2 - 1} dz$$

wehre C is the contour 2-1/2-1

Alation [4] Alatha and a second Find the map of straight line y = x under the transformation (c)

$$w = \frac{z-1}{z+1}.$$