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S.E. (Computer/IT Engineering) (Second Semester)

EXAMINATION, 2017

ENGINEERING MATHEMATICS III

(2015 Course)

Time: Two Hours

Maximum Marks: 50

N.B. :- (i) Neat diagrams must be drawn wherever necessary.

- (ii) Figures to the right indicate full marks.
- (iii) Your answers will be valued as a whole.
- (iv) Use of electronic pocket calculator is allowed.
- (v) Assume suitable data, if necessary.
- (a) Solve any two: 1.

[8]

Solve any
$$two$$
:
(i) $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 2e^{e^x}$

(ii) (D² + 4D + 4)y =
$$x^{-3} e^{-2x}$$

(iii)
$$x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$$

Find the Fourier transform of: (b)

[4]

Find the Fourier transform of:
$$f(x) = 1, |x| \le 1$$

$$= 0, |x| > 1$$
and evaluate
$$\int_0^\infty \frac{\lambda \cos \lambda x}{\lambda} d\lambda.$$

and evaluate
$$\int_0^\infty \frac{\lambda \cos \lambda x}{\lambda} d\lambda$$
.

- 2. (a) An inductor of 0.5 henries is connected in series with a registor of 6 ohms, a capacitor of 0.02 farads, a generator having alternative voltage given by 24 sin 10 t, t > 0 and switch k. Set up a differential equation for this circuit and find charge at time t. [4]
 - (b) Solve any one of the following: $(i) \quad \text{Find } z\{f(k)\}, \text{ where } f(k) = 3^k, k < 0$ $= 2^k, k \ge 0$
 - (ii) Find:

$$z^{-1}\left\{\frac{z^2}{z^2+1}\right\}$$

by using inversion integral method.

- (c) Solve the following difference equation: y(k + 2) 5y(k + 1) + 6y(k) = 36y(0) = y(1) = 0.
- 3. (a) Calculate the first four central moments from the following data and hence find β_1 and β_2 : [4]

x	0	1	2	3	4	5	6
f	5	15	17	25	19	1.4	5

(b) Fit a straight line to the following data by least square method: [4]

x	0	5	10	15	20	25
y	12	15	17	22	24	30

(c)	The number of breakdowns of a computer in a week is a
	Poisson variable with $\lambda = np = 0.3$. What is the probability
	that the computer will operate: [4]
1	(i) with no breakdown and
	(ii) at the most one breakdown in a week. Or
(a)	The average test marks in a particular class is 79 and standard
	deviation is 5. If the marks are normally distributed, how many
	students in a class of 200, did not receive marks between
	75 and 82. Given $z = 0.8$, Area = 0.2881 and $z = 0.6$,
	Area = 0.2257 . [4]
(<i>b</i>)	An insurance agent accepts policies of 5 men of identical age
	and in good health. The probability that a man of this age
	will be alive 30 years hence is 2/3. Find the probability that
	in 30 years: [4]
	(i) all five men and
	(ii) at least one man will be alive.
(c)	The two variables x and y have regression lines: [4]
	3x + 2y - 26 = 0 and $6x + y - 31 = 0$
	Find:
	(i) the mean values of x and y and
	(ii) correlation coefficient between x and y.
(a)	Find the directional derivative of a scalar point function
	$\phi = xy^2 + yz^3$ at $(2, -1, 1)$ in the direction of a vector
	Ai + 2i + 4b

P.T.O.

4.

5.

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Show that the vector field: (b)

$$\overline{F} = (6xy + z^3)i + (3x^2 - z)j + (3xz^2 - y)k$$

is irrotational and hence find a scalar potential function φ such that $\overline{F} = \nabla \phi$. [4]

Find the work done by the vector field: (c)[5] $F = (x^{2} - yz)i + (y^{2} - zx)j + (z^{2} - xy)k$ in moving a particle of unit mass from (1, 1, 1) to (2, -1, 2).

Or

Find the directional derivative of a scalar point function 6. $\phi = xy - z^2 + 2xz$ at (1, 0, 2) in the direction of 4i - j[4]

Show that (any one): [4]

 $\nabla \left(\frac{\overline{a}.\overline{r}}{r^n} \right) = \frac{\overline{a}}{r^n} - \frac{n(\overline{a},\overline{r})\overline{r}}{r^{n+2}}, \text{ where } \overline{a} \text{ is a constant vector.}$

$$(ii) \quad \nabla^2 \left(\nabla \cdot \frac{\overline{r}}{r^2} \right) = \frac{2}{r^4}$$

- Evaluate the integral $\int_{c}^{\overline{F}. d\overline{r}}$, along the curve x = 2t, y = t, z = 3t from t = 0 to t = 1, where $\overline{F} =$ $3x^2i$ + (2xz - y)j + zk.[5]
- 7. If: (α)

$$u = -2xy + \frac{y}{x^2 + y^2},$$

 $u = -2xy + \frac{y}{x^2 + y^2},$ that $f(z) = u^{-1}$ find v such that f(z) = u + iv is analytic. Determine f(z) in [4]terms of z.

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Evaluate $\oint_{c} \frac{e^{z}}{(z+1)(z+2)} dz$, where c is the contour

$$|z + 1| = \frac{1}{2}.$$
 [5]

Find the Bilinear transformation which maps the point (c) -i, 0, 2 + i of the z-plane onto the points 0, -2i, 4 of the w-plane. [4]

Or

(a)8.

$$u = \frac{1}{2}\log(x^2 + y^2),$$

find v such that f(z) = u iv is analytic. Determine f(z) in terms of zterms of z.

Evaluate $\oint_C \frac{\sin \pi z^2 + 2z}{(z-1)(z-2)} dz$, where c is the circle |z| = 4. (b)

[5]

Find the image of the circle $(x - 3)^2 + y^2 = 2$ under the (c) A STATE OF THE STA transfromation $\psi = \frac{1}{z}$.